

Geometry Honors

Name: \_\_\_\_\_  
 Period: \_\_\_\_\_

Key

1. Find the measure of an angle and its supplement if the angle is  $15^\circ$  less than twice its supplement.

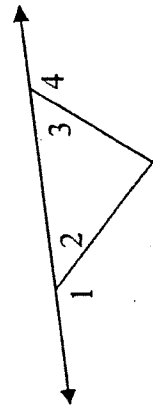
let  $x = \text{meas. of } \angle$   
 $180 - x = \text{supp}$

$$\begin{aligned} x &= 2(180 - x) - 15 \\ x &= 360 - 2x - 15 \\ 3x &= 345 \\ x &= 115 \end{aligned}$$

$$\begin{array}{r} \text{ck: } 65 \times 2 = 130 \\ -15 \\ \hline 115^\circ \end{array}$$

$\{115^\circ, 65^\circ\}$

2. Given:  $\angle 1 \text{ supp } \angle 2$   
 $\angle 2 \cong \angle 3$   
 $\angle 4 \text{ supp } \angle 3$



Prove:  $\angle 1 \cong \angle 4$

$$\begin{aligned} \textcircled{1} \angle 1 \text{ Supp } \angle 2 &\rightarrow \textcircled{2} m\angle 1 + m\angle 2 = 180 \rightarrow \textcircled{3} m\angle 1 + m\angle 2 = m\angle 4 + m\angle 3 \\ \angle 4 \text{ Supp } \angle 3 &\rightarrow m\angle 4 + m\angle 3 = 180 \rightarrow \textcircled{4} \angle 2 \cong \angle 3 \rightarrow \textcircled{5} m\angle 2 = m\angle 3 \end{aligned}$$

$$\textcircled{6} m\angle 1 + m\angle 2 = m\angle 4 + m\angle 2 \rightarrow \textcircled{7} m\angle 1 = m\angle 4 \rightarrow \textcircled{8} \angle 1 \cong \angle 4$$

(Optional)

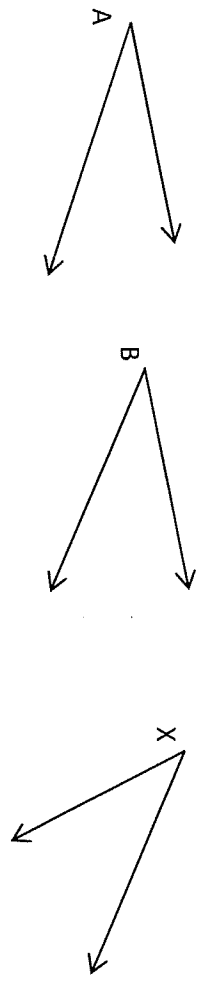
Reasons

- $\textcircled{1}$  Given
- $\textcircled{2}$  Suppl.  $\angle$ s are  $2 \angle$ 's that totals 180.
- $\textcircled{3}$  Substitution Prop.
- $\textcircled{4}$  Given
- $\textcircled{5}$   $\cong \angle$ 's have = measures.
- $\textcircled{6}$  Substitution Prop.
- $\textcircled{7}$  Substitution Prop.
- $\textcircled{8}$   $\cong \angle$ 's have = measures.

**Congruent complements theorem:** If two angles complement the same angle or are complementary to congruent angles, then the two angles are congruent.  $\longrightarrow$   $\angle$ s that complement the same  $\angle$ s are congruent.

Given:  $\angle A$  complement  $\angle X$   
 $\angle B$  complement  $\angle X$ .

Prove:  $\angle A \cong \angle B$



$$\begin{aligned} \textcircled{1} \angle A \text{ compl. } \angle X &\longrightarrow \textcircled{2} m\angle A + m\angle X = 90^\circ \\ \angle B \text{ compl. } \angle X &\longrightarrow m\angle B + m\angle X = 90^\circ \end{aligned} \left. \vphantom{\begin{aligned} \textcircled{1} \angle A \text{ compl. } \angle X \\ \angle B \text{ compl. } \angle X \end{aligned}} \right\} \longrightarrow \textcircled{3} m\angle A + m\angle X = m\angle B + m\angle X$$

$$\textcircled{4} m\angle A = m\angle B \longrightarrow \textcircled{5} \angle A \cong \angle B$$

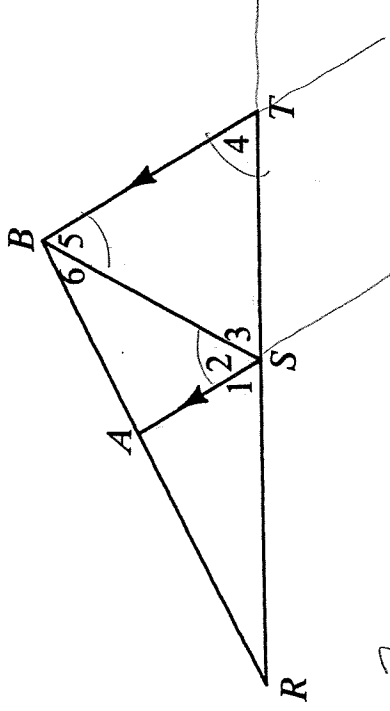
- ① Given
- ② Compl.  $\angle$ s are 2  $\angle$ s whose sum is  $90^\circ$ .
- ③ Substitution Prop.
- ④ Subtraction Prop.
- ⑤  $\cong$   $\angle$ s have = measures.

5. Given:  $\overline{AS} \parallel \overline{BT}$ ;

$$m\angle 4 = m\angle 5$$

Prove:  $\overrightarrow{SA}$  bisects  $\angle BSR$ .

Plan: Show  $\angle 1 \cong \angle 2$

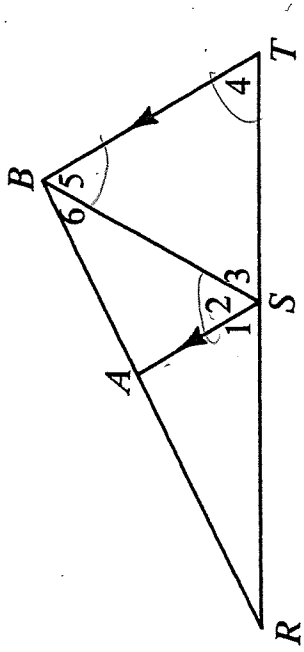


- ①  $\overline{AS} \parallel \overline{BT} \rightarrow$  ②  $\angle 5 \cong \angle 2$   $\rightarrow$  ⑤  $\angle 2 \cong \angle 4$
- ③  $m\angle 4 = m\angle 5 \rightarrow$  ④  $\angle 4 \cong \angle 5$   $\rightarrow$  ⑥  $\angle 1 \cong \angle 4$
- $\rightarrow$  ⑦  $\angle 1 \cong \angle 2$   $\rightarrow$  ⑧  $\overrightarrow{SA}$  bisects  $\angle BSR$ .

- ① Given
- ② 2  $\parallel$  lines  $\rightarrow$  alternate interior  $\angle$ s  $\cong$
- ③ Given
- ④ If  $\angle$ s are  $\cong$ , they are  $\cong$ .
- ⑤ Transitive Property
- ⑥ 2  $\parallel$  lines  $\rightarrow$  corresp.  $\angle$ s  $\cong$ .
- ⑦ Transitive Prop.
- ⑧ Def. of  $\angle$  bisector: If a ray creates 2  $\cong$   $\angle$ s, then it is an  $\angle$  bisector.



6. Given:  $\overline{AS} \parallel \overline{BT}$ ;  
 $m\angle 4 = m\angle 5$ ;  
 $\overrightarrow{SB}$  bisects  $\angle AST$ .  
 Find the measure of  $\angle 1$ .



Because  $\overline{AS} \parallel \overline{BT}$ ,  $\angle 2 \cong \angle 4$

Given  $m\angle 4 = m\angle 5 \rightarrow \angle 4 \cong \angle 5$

so,  $\angle 2 \cong \angle 4$

so,  $\angle 3 \cong \angle 4$

Since  $\overline{SB}$  bisects  $\angle AST$ ,  $\angle 2 \cong \angle 3$

Now,  $\angle 3 \cong \angle 4 \cong \angle 5$ .  $\triangle BST$  is equilateral;  $m\angle 4 = 60^\circ$ .

Since  $\angle 1$  &  $\angle 4$  are corresponding  $\angle$ s formed by  $\parallel$  lines,

$\angle 1 \cong \angle 4$ . Therefore  $m\angle 1 = 60^\circ$ .

