Quadratics 2.1 Writing equations of Transformations of Quadratic Functions

Question: Is the order of the transformations important?

Example 1: The function $y=x^2$ undergoes a vertical stretch by a factor of 2, then a reflection across the x-axis, and then a translation 3 units down. Write a rule for g, the new function, and identify the vertex. Check with your calculator.

①
$$h(x) = 2x^{2}$$

② $h(x) = -2x^{2}$
③ $g(x) = -2x^{2} - 3$
 $\Rightarrow g(x) = -2(x-0)^{2} - 3$

Example 2: The function $\widehat{\psi} = x^2$ is translated 3 units down, then reflected across the x-axis, followed by a vertical stretch by a factor of 2. Write a rule for g, the new function, and identify the vertex. Check with your calculator.

$$h(x) = x^2 - 3$$

(2)
$$h(x) = -(x^2 - 3)$$

= $-x^2 + 3$

(3)
$$h(x) = 2(-x^2 + 3)$$

Example 3: Let the graph of g be a translation 3 units right and 2 units up, followed by a reflection in the yaxis of the graph of $f(x) = x^2 - 5x$. Write a rule for g.

(4) Reflection =
$$h(-x) = (-x)^2 - 11(-x) + 26$$

D h(X)= f(X-3)+2 ← dift f up 2K

(b) final:
$$g(x) = X^2 + 1(x + 26)$$

Ex2 (1) y= X 2 YZXZ (2) Vertical shetch y= 2x² (factor of 2)

(3) reflection x-axis y=-2x² 2) translate 3 down reflect x-axis $y = -(x^2-3)$ $y = -x^2+3$ Vertical shetch $y=2(-x^2+3)$ Factor of $\lambda = -2x^2+6$ Fanslate 3 down y=-2x2-3 10 Y=2X2 @ P/NHL FINAL

PRACTICE:

1. Let the graph of g by a vertical shrink by a factor of ½ followed by a translation 2 units up of the graph of $f(x) = x^2$. Write a rule for g and identify the vertex.

$$h(x) = \frac{1}{2}x^2$$

$$g(x) = \frac{1}{2}x^2 + 2$$

2. Carry out problem #1 but reverse the order of transformations. Write a rule for g and identify the vertex.

$$h(x) = X^{2} + 2$$

 $g(x) = \pm (x^{2} + 2)$

- vertex (0,1) > |q(x)= = x2+1
- 3. Let the graph of g be a translation 4 units left followed by a vertical shrink by a factor of 1/3 of the graph of $f(x) = x^2 + x$. Write a rule for g and identify the vertex.

$$h(x) = X^{2} + X$$

$$= (x + 4)^{2} + (x + 4)$$

$$= X^{2} + 8x + 16 + X + 4$$

$$= \chi^{2} + \chi$$

$$= (\chi + 4)^{2} + (\chi + 4)$$

$$= (\chi + 4)^{2} + (\chi + 4)$$

$$= \chi^{2} + 8\chi + 16 + \chi + 4$$

$$= \chi^{2} + 9\chi + 20$$

$$= \chi^{2} + 9\chi + 20$$

$$= \chi^{2} + 9\chi + 20$$

$$= -9$$

$$= (\chi + 4)^{2} + (\chi + 4)$$

$$= (\chi + 4)^{2} + (\chi + 4)^{2} + (\chi + 4)$$

$$= (\chi + 4)^{2} + (\chi + 4)^{2}$$

 $= \chi^2 + 9\chi + 2O$ $= -\frac{9}{2}$ $\frac{1}{3}(-\frac{8}{4} + \frac{80}{4}) \Rightarrow \frac{1}{3}(-\frac{4}{4})$ Write a function g based on the transformations of $f(x) = 2x^2 + 6x$: a translation 6 units down followed by a reflection in the x-axis. Write a rule for g and identify the vertex.

$$h(x) = 2x^{2} + 6x - 6$$

$$h(x) = -(2x^{2} + 6x - 6)$$

$$g(x) = -2x^{2} - 6x + 6$$

$$Vextex (-\frac{2}{2}, \frac{21}{2})$$

$$x = \frac{6}{4} = -\frac{2}{2}$$

$$y = -2(\frac{9}{4}) - 6(-\frac{3}{2}) + 6$$

$$= -\frac{9}{4} + 9 + 6 \rightarrow 10\dot{z} = \frac{21}{2}$$

Write a function g based on the transformations of $f(x) = 2x^2 + 6x$: a reflection in the y-axis followed by a translation 4 units right. $g(x) = 2x^2 - 22x + 56$

$$0 h(-x) = 2(-x)^{2} + 6(-x)$$

$$= 2x^{2} - 6x$$

$$2h(x-4) = 2(x-4)^{2} - 6(x-4)$$

$$= 2(x^{2} - 8x + 16) - 6x + 24$$

$$= 2x^{2} - 16x + 32 - 6x + 24$$