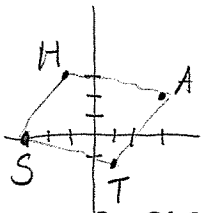


Geometry (H)
Section 5.4 – Identifying Quads in the Coordinate Plane

Directions: Graph each quadrilateral then determine the type of quadrilateral: rectangle, rhombus, square or parallelogram. Join the vertices in the given order. ~~Use~~ must use slope or distance to verify the type of quadrilateral.

1. H(-1,3) A(3,2) T(1,-1) S(-3,0)



$$m_{\overline{HS}} = \frac{3-0}{-1+3} = \frac{3}{2}$$

$$m_{\overline{ST}} = \frac{-1-0}{1+3} = -\frac{1}{4}$$

not \perp .

$$d_{\overline{HA}} = \sqrt{(-1-3)^2 + (3-2)^2} = \sqrt{16+1} = \sqrt{17}$$

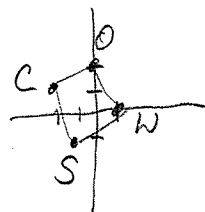
$$d_{\overline{ST}} = \sqrt{(1+3)^2 + (-1-0)^2} = \sqrt{16+1} = \sqrt{17}$$

$$d_{\overline{HS}} = \sqrt{(-1+3)^2 + (3-0)^2} = \frac{\sqrt{4+9}}{\sqrt{4+9}} = \sqrt{13}$$

$$d_{\overline{AT}} = \sqrt{(3-1)^2 + (2+1)^2} = \frac{\sqrt{4+9}}{\sqrt{4+9}} = \sqrt{13}$$

Since $\overline{HA} \cong \overline{ST}$ and $\overline{HS} \cong \overline{AT}$, HATS is a parallelogram.

3. C(-2,1) O(0,2) W(1,0) S(-1,-1)



$$m_{\overline{CW}} = \frac{1-0}{-2-1} = -\frac{1}{3}$$

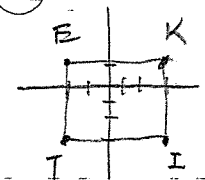
$$m_{\overline{OS}} = \frac{2+1}{0+1} = \frac{3}{1}$$

$$d_{\overline{OS}} = \sqrt{(0+1)^2 + (2+1)^2} = \sqrt{1+9} = \sqrt{10}$$

$$d_{\overline{CW}} = \sqrt{(-2-1)^2 + (1-0)^2} = \sqrt{9+1} = \sqrt{10}$$

$\overline{CW} \perp \overline{OS}$ and $\overline{OS} \cong \overline{CW}$, therefore, COWS is a square.

4. K(3,1) I(3,-3) T(-2,-3) E(-2,1)



$$d_{\overline{EK}} = \sqrt{(3+2)^2 + (1-1)^2} = \sqrt{25} = 5$$

$$d_{\overline{TI}} = \sqrt{(3+2)^2 + (-3+3)^2} = \sqrt{25} = 5$$

$$d_{\overline{ET}} = \sqrt{(-2+2)^2 + (-3-1)^2} = \sqrt{0+16} = 4$$

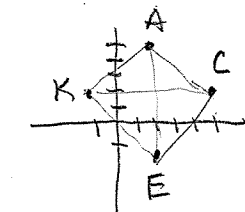
$$d_{\overline{KI}} = \sqrt{(3-3)^2 + (1+3)^2} = \sqrt{0+16} = 4$$

$$m_{\overline{EK}} = \frac{1-1}{3+2} = 0$$

$$m_{\overline{ET}} = \frac{-3-1}{-2+2} = \frac{-4}{0}$$

$\overline{EK} \cong \overline{TI}$, $\overline{ET} \cong \overline{KI}$, KITE is a kite.

6. C(5,2) A(2,5) K(-1,2) E(2,-1)



Square

$$m_{\overline{AE}} = \frac{5+1}{2-2} = \frac{6}{0} = \text{undef}$$

$$m_{\overline{KC}} = \frac{2-2}{5+1} = \frac{0}{6} = 0$$

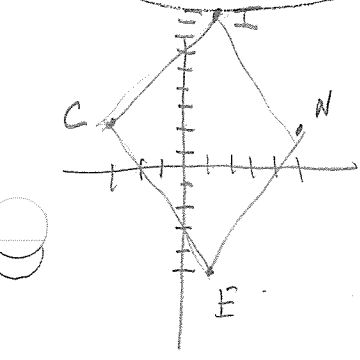
$$d_{\overline{AE}} = \sqrt{(2-2)^2 + (5+1)^2} = \sqrt{36} = 6$$

$$d_{\overline{KC}} = \sqrt{(5+1)^2 + (2-2)^2} = \sqrt{36} = 6$$

So, $\overline{AE} \perp \overline{KC}$ and $\overline{AE} \cong \overline{KC}$, Square

7. N(5,2) I(1,9) C(-3,2) E(1,-5)

Rhombus



$$m_{\overline{CN}} = \frac{2-2}{5+3} = 0$$

$$m_{\overline{IE}} = \frac{9+5}{1-1} = \frac{14}{0} = \text{undef}$$

$\overline{CN} \perp \overline{IE}$

$\overline{CI} \cong \overline{CE} \cong \overline{IN} \cong \overline{NE}$

$$d_{\overline{CI}} = \sqrt{(1+3)^2 + (9-2)^2} = \sqrt{16+49} = \sqrt{65}$$

$$d_{\overline{IN}} = \sqrt{(5-1)^2 + (2-9)^2} = \sqrt{16+49} = \sqrt{65}$$

$$d_{\overline{CE}} = \sqrt{(-3-1)^2 + (2+5)^2} = \sqrt{16+49} = \sqrt{65}$$

$$d_{\overline{NE}} = \sqrt{(5-1)^2 + (2+5)^2} = \sqrt{16+49} = \sqrt{65}$$

Geometry (H)
Section 5.4 – Special Parallelogram continued ...

Name: KEY

1. Put an X in the box if the shape has the given properties.

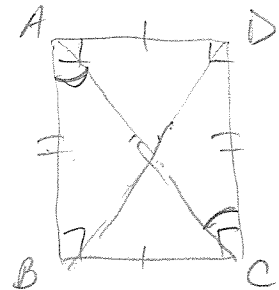
Property	Parallelogram	Rectangle	Rhombus	Square
Both pairs of opposite sides //	X	X	X	X
Diagonals are \perp			X	X
Diagonals are \cong		X		X
Diagonals bisect each other	X	X	X	X
All angles are right angles		X		X
One pair of opposite sides \cong				
All sides are \cong			X	X
Both pairs of opposite angles \cong	X	X	X	X
Diagonals bisect the angles they are drawn from			X	X
All angles are \cong		X		X

2. Let's prove the properties we discovered yesterday!

Thm: The diagonals of a rectangle are congruent.

Given: rectangle ABCD

Diagram:



Prove: $\overline{AC} \cong \overline{BD}$

Prove: $\triangle AOC \cong \triangle DOB$ (overlap) (SAS)

① Rectangle ABCD \rightarrow ② $\overline{AB} \cong \overline{DC}$

\rightarrow ③ $\angle ABC$ & $\angle DCB$ are right \angle s. \rightarrow ④ $\angle ABC \cong \angle DCB$ \rightarrow ⑥ $\triangle ABC \cong \triangle DCB$ \rightarrow ⑦ $\overline{AC} \cong \overline{BD}$

⑤ $\overline{BC} \cong \overline{BC}$

① Given

③ Def. of rectangle

⑤ Reflexive Prop.

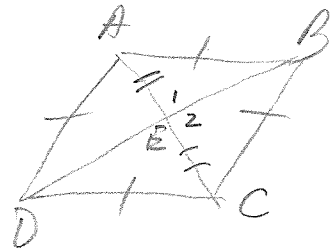
⑦ CPCTC

② Rect. \rightarrow opp sides \cong . ④ All right \angle s \cong ⑥ SAS \cong SAS

Thm: The diagonals of a rhombus are perpendicular.

Given: rhombus ABCD

Diagram:



Prove: $\overline{AC} \perp \overline{BD}$

Prove: $\triangle ABE \cong \triangle CBE$ (SSS)

Use "if 2 lines form \cong adj. \angle s, then 2 lines \perp ."

① Rhombus ABCD \rightarrow ② $\overline{AB} \cong \overline{BC}$
 \rightarrow ③ \square ABCD \rightarrow ④ \overline{AC} & \overline{BD} bisect each other \rightarrow ⑤ $\overline{AE} \cong \overline{EC}$
 ⑥ $\overline{BE} \cong \overline{BE}$ } ⑦ $\triangle ABE \cong \triangle CBE$
 \rightarrow ⑧ $\angle 1 \cong \angle 2 \rightarrow$ ⑨ $\overline{AC} \perp \overline{BD}$

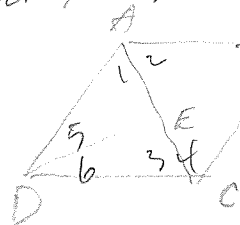
① Given
 ② Rhombus \rightarrow all sides \cong
 ③ Def of a rhombus: \square w/ 4 \cong sides
 ④ \square \rightarrow diag. bisect each other
 ⑤ Def. of bisector
 ⑥ Reflexive Prop.
 ⑦ SSS \cong SSS
 ⑧ CPCTC
 ⑨ If 2 lines form \cong adj. \angle s, then lines \perp .

Thm: Each diagonal of a rhombus bisects the angles they are drawn from.

If a quad. is a rhombus, then each diag. bisect the \angle s they are drawn from.

Given: rhombus ABCD

Diagram:



Prove: \overline{AC} bisects $\angle DAB$ & $\angle BCD$
 \overline{BD} bisects $\angle ADC$ & $\angle ABC$

① Rhomb ABCD \rightarrow ② $\overline{AB} \cong \overline{BC} \cong \overline{CD} \cong \overline{DA}$
 ③ $\overline{BD} \cong \overline{BD}$ } \rightarrow ④ $\triangle ABD \cong \triangle CBD \rightarrow$ ⑤ $\angle 5 \cong \angle 6$
 $\angle 7 \cong \angle 8$
 ⑥ \overline{BD} bis. $\angle ADC$ & $\angle ABC$
 ⑦ $\overline{AB} \cong \overline{BC} \cong \overline{CD} \cong \overline{DA}$
 ⑧ $\overline{AC} \cong \overline{AC}$ } \rightarrow ⑨ $\triangle ADC \cong \triangle ABC \rightarrow$ ⑩ $\angle 1 \cong \angle 2$
 $\angle 3 \cong \angle 4$

① Given
 ② In a rhombus, all sides \cong .
 ③ Reflexive property
 ④ SSS \cong SSS
 ⑤ CPCTC
 ⑥ Def. \angle bisector
 ⑦ same as #2
 ⑧ Reflexive prop.
 ⑨ SSS \cong SSS
 ⑩ CPCTC
 ⑪ Def \angle bisector
 ⑪ \overline{AC} bis. $\angle DAB$ & $\angle BCD$