

Topic: Quadratic Inequalities

Today, we will...

- (1) graph quadratic inequalities in two variables
- (2) graph a system of quadratic inequalities
- (3) solve a quadratic inequality algebraically
- (4) solve a quadratic inequality by graphing

1. Graph quadratic inequalities in two variables

$y < -x^2 - 8x - 2$ ^① Graph $y = -x^2 - 8x - 2$

vertex: $x = \frac{-b}{2a} = -4$

$y = -16 + 32 - 2 = 14$

vertex $(-4, 14)$

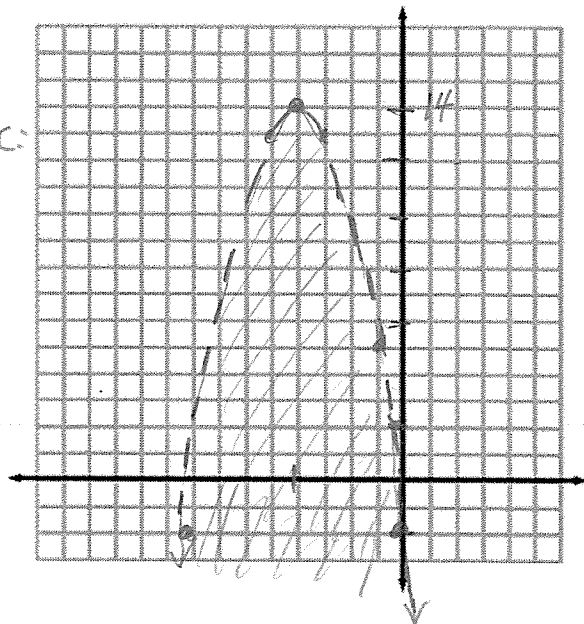
y-int $(0, -2)$

sym pt $(-8, -2)$

② Pick a pt & check:
 $(-2, 0)$

$0 < -4 + 16 - 2$
?

$0 < 10$
✓



2. Graph a system of inequalities

$y < -x^2 + 3$
 $y \geq x^2 + 2x - 3$

do by transformations or vertex

$y = x^2 + 2x - 3$

$x = \frac{-2}{2} = -1$

$y = 1 - 2 - 3 = -4$

vertex $(-1, -4)$

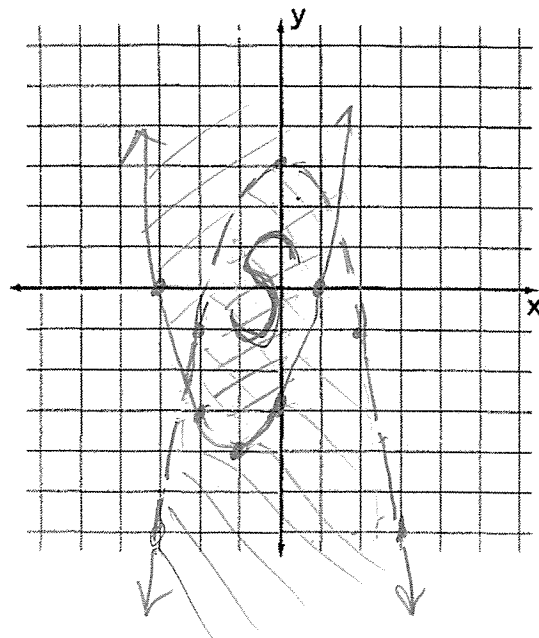
y-int $(0, -3)$

sym pt $(-2, -3)$

roots =

$0 = (x+3)(x-1)$

$x = -3 \quad x = 1$

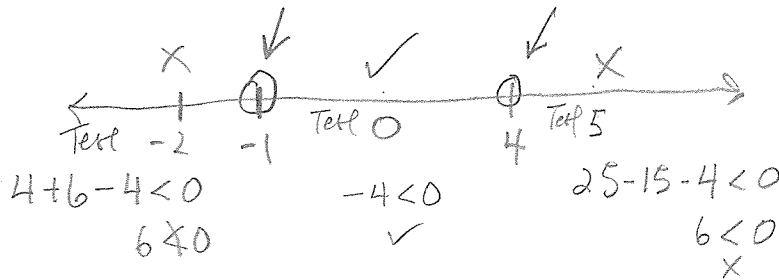


3. Solve a quadratic inequality algebraically

Solve algebraically: $x^2 - 3x - 4 < 0$

① Find x-intercepts for $x^2 - 3x - 4 = 0$
 $(x-4)(x+1) = 0$
 $x = 4 \quad x = -1$

② Make a # line & check each section.



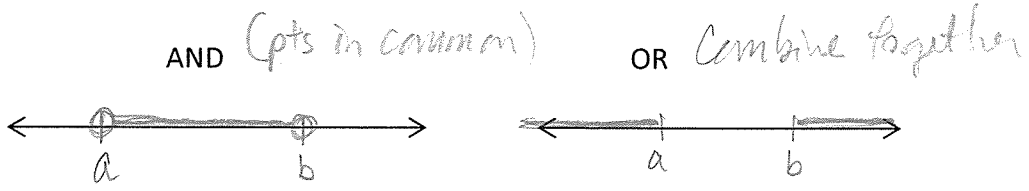
③ State solution statement.

$-1 < x < 4$

4. Solve a quadratic inequality by graphing

(note: "less thAND" and "greatOR" still work here)

Quick review: If "a" and "b" are the roots to the equation....



Solve by graphing:

$3x^2 - x - 5 \geq 0$

$3x^2 - x - 5 = y$

vertex: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$y = 3\left(\frac{1}{6}\right)^2 - \frac{1}{6} - 5$
 $= \frac{1}{12} - \frac{2}{12} - \frac{60}{12}$
 $= \frac{-61}{12} = -5\frac{1}{12}$

$\left(\frac{1}{6}, -5\frac{1}{12}\right)$

y-int: $(0, -5)$

sympt pt: $\left(\frac{1}{3}, -5\right)$

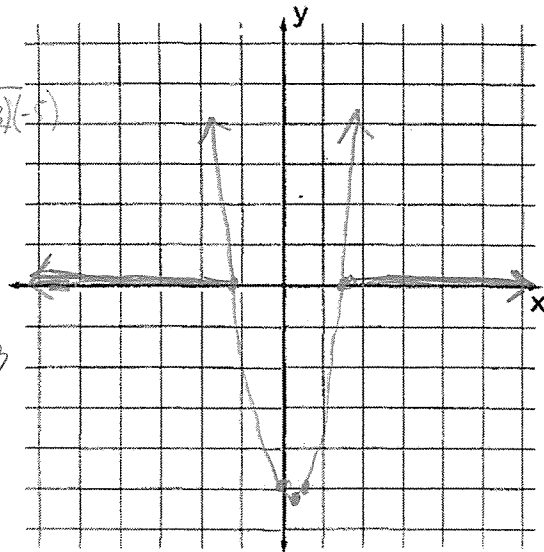
$3x^2 - x - 5 = 0$

$x = \frac{1 \pm \sqrt{1 - 4(3)(-5)}}{6}$

$\frac{1 \pm \sqrt{61}}{6}$

$x \approx 1.46$

$x \approx -1.13$



check: $x = 2$

$3(4) - 2 - 5 \geq 0$

$5 \geq 0$

✓

$x = -2$

$12 + 2 - 5 \geq 0$

$9 \geq 0$

✓

$x \leq -1.13 \text{ or } x \geq 1.46$

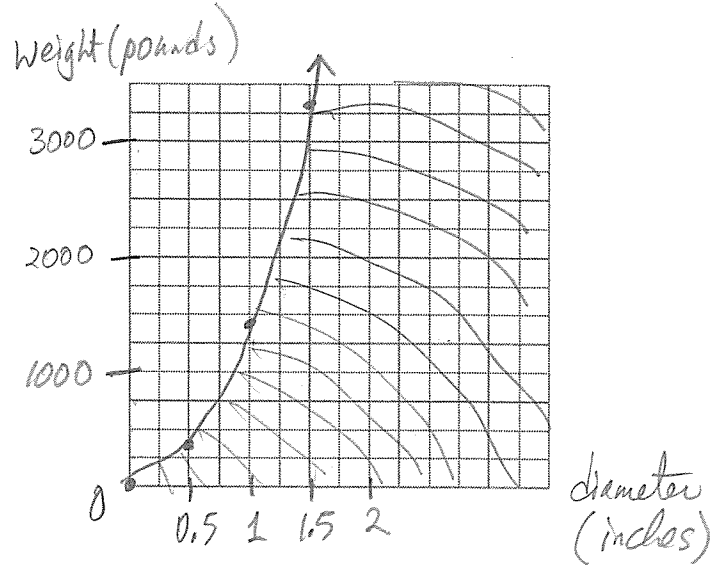
Topic: Quadratic Inequalities - Application problems

1. A manila rope used for rappelling down a cliff can safely support a weight W (in pounds) provided $1480d^2 \geq W$ where d is the diameter (in inches) of the rope. Graph the inequality and interpret the solution.

Graph: $W = 1480d^2$
 \swarrow x

d	W
0.5	370
1	1480
1.5	3330
2	5920

Test (1,0)
 $1480 \geq 0$
 ✓



2. A rectangular parking lot must have a perimeter of 440 feet and an area of at least 8000 square feet. Describe the possible lengths of the parking lot. After setting up your equations/inequalities, use your graphing calculator. Copy the graph from your calculator.

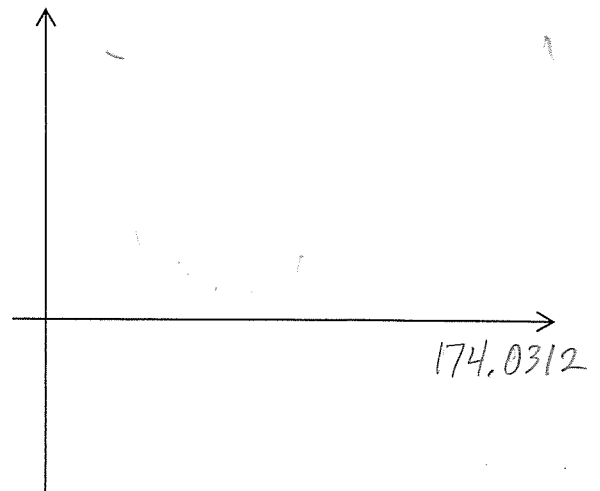
$$2L + 2W = 440 \rightarrow L + W = 220$$

$$LW \geq 8000 \quad L = 220 - W$$

$$W(220 - W) \geq 8000$$

$$220W - W^2 \geq 8000$$

$$-W^2 + 220W - 8000 \geq 0$$



Topic: Quadratic Inequalities - Practice Problems

1. Solve this system by graphing.

$$y \geq x^2$$

$$2x + y < 8$$

$$y \geq x^2$$

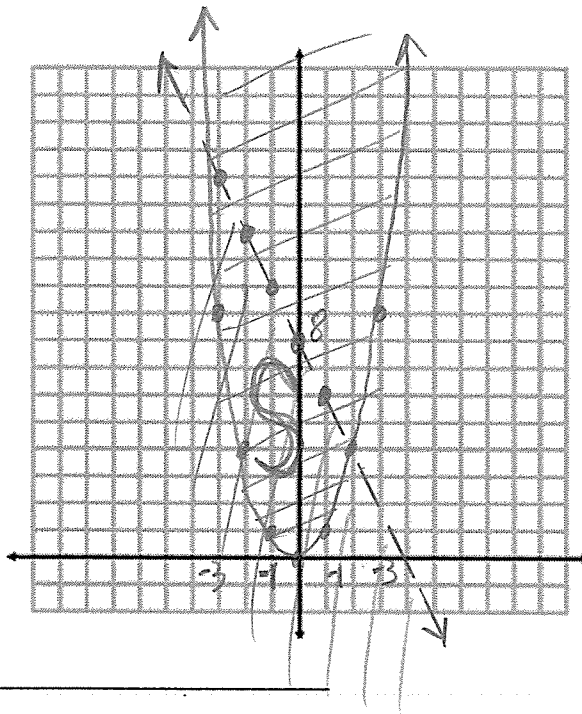
Test (0,1)

$$1 \geq 0 \checkmark$$

$$y = -2x + 8$$

Test (0,0)

$$0 < 8 \checkmark$$



Solution statement(s) _____

2. $y \leq 2x + 10$

$$y \geq -x^2 - 4x + 1$$

Test (0,0)

$$0 \leq 10 \checkmark$$

$$y = -x^2 - 4x + 1$$

$$x = \frac{-b}{2a} = -2$$

$$y = -4 + 8 + 1$$

$$y = 5$$

vertex (-2, 5)

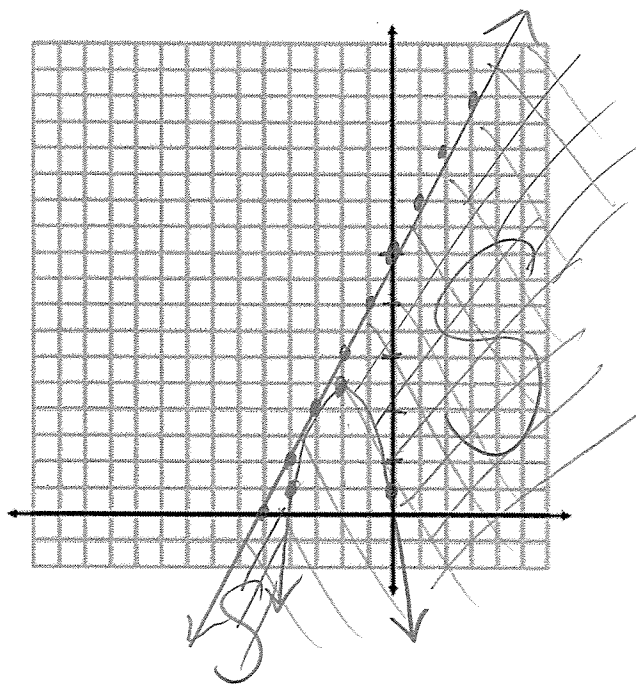
y-int (0, 1)

Sym pt (-4, 1)

Test (-1, 0)

$$0 \geq -1 + 4 + 1$$

$$0 \geq 4 \text{ X}$$



Solution statement(s) _____

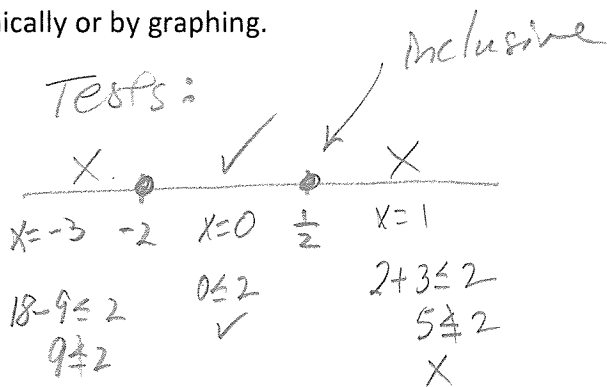
Solve these inequalities algebraically or by graphing.

3. $2x^2 + 3x \leq 2$

$$2x^2 + 3x - 2 = 0$$

$$(2x - 1)(x + 2) = 0$$

$$x = \frac{1}{2} \quad x = -2$$



Solution $\left\{ -2 \leq x \leq \frac{1}{2} \right\}$

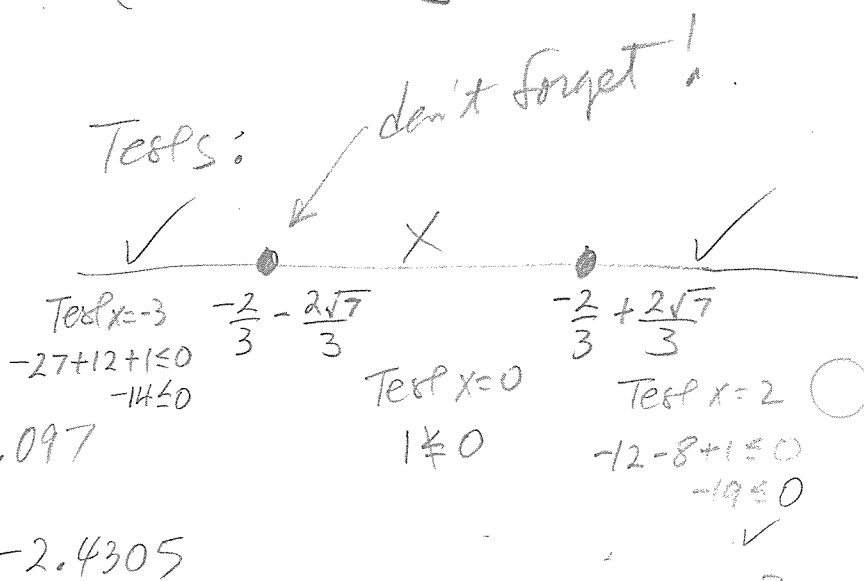
4. $-3x^2 - 4x + 1 \leq 0$

$$-3x^2 - 4x + 1 = 0$$

$$x = \frac{4 \pm \sqrt{16 - 4(-3)(1)}}{2(-3)}$$

$$= \frac{4 \pm \sqrt{28}}{-6}$$

$$= -\frac{2}{3} \pm \frac{\sqrt{7}}{3}$$



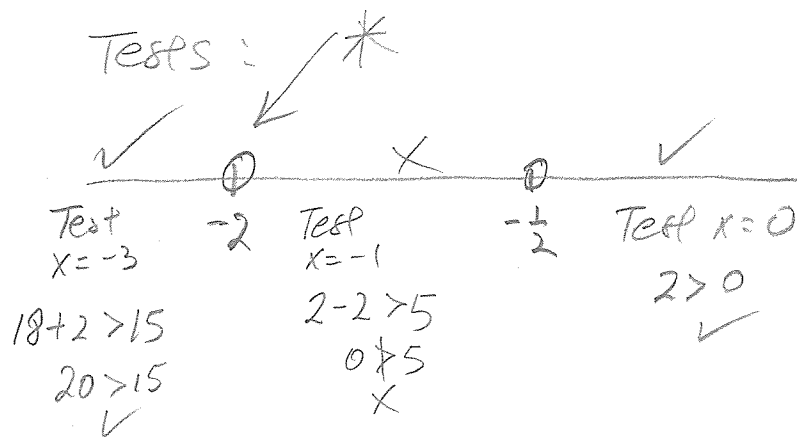
5. $2x^2 + 2 > -5x$

$$2x^2 + 5x + 2 = 0$$

$$(2x + 1)(x + 2) = 0$$

$$x = -\frac{1}{2} \quad x = -2$$

$S = \left\{ x \leq -\frac{2}{3} - \frac{\sqrt{7}}{3} \text{ or } x \geq -\frac{2}{3} + \frac{\sqrt{7}}{3} \right\}$



$S: \left\{ x < -2 \text{ or } x > -\frac{1}{2} \right\}$